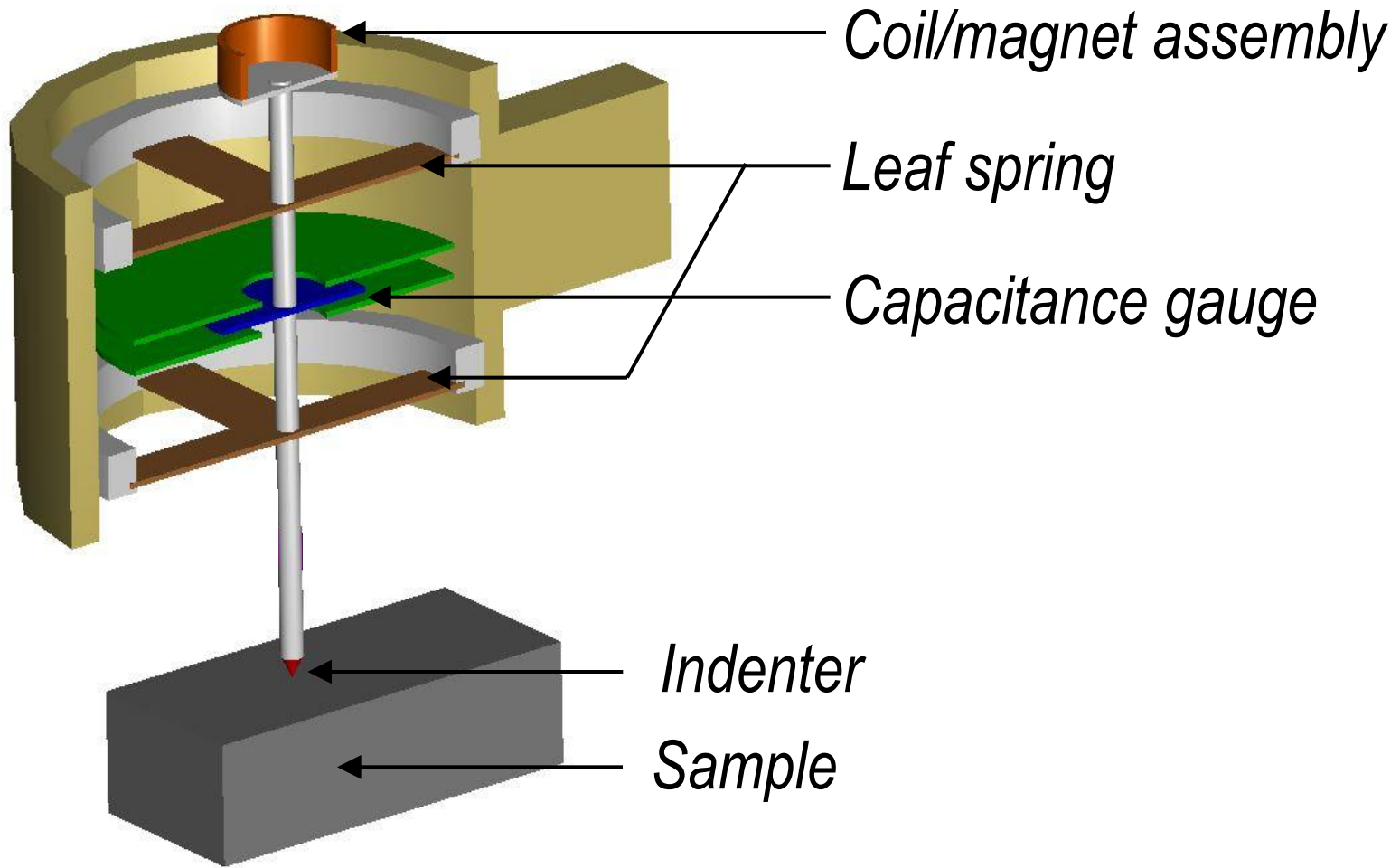


Continuous Stiffness Measurements (CSM)

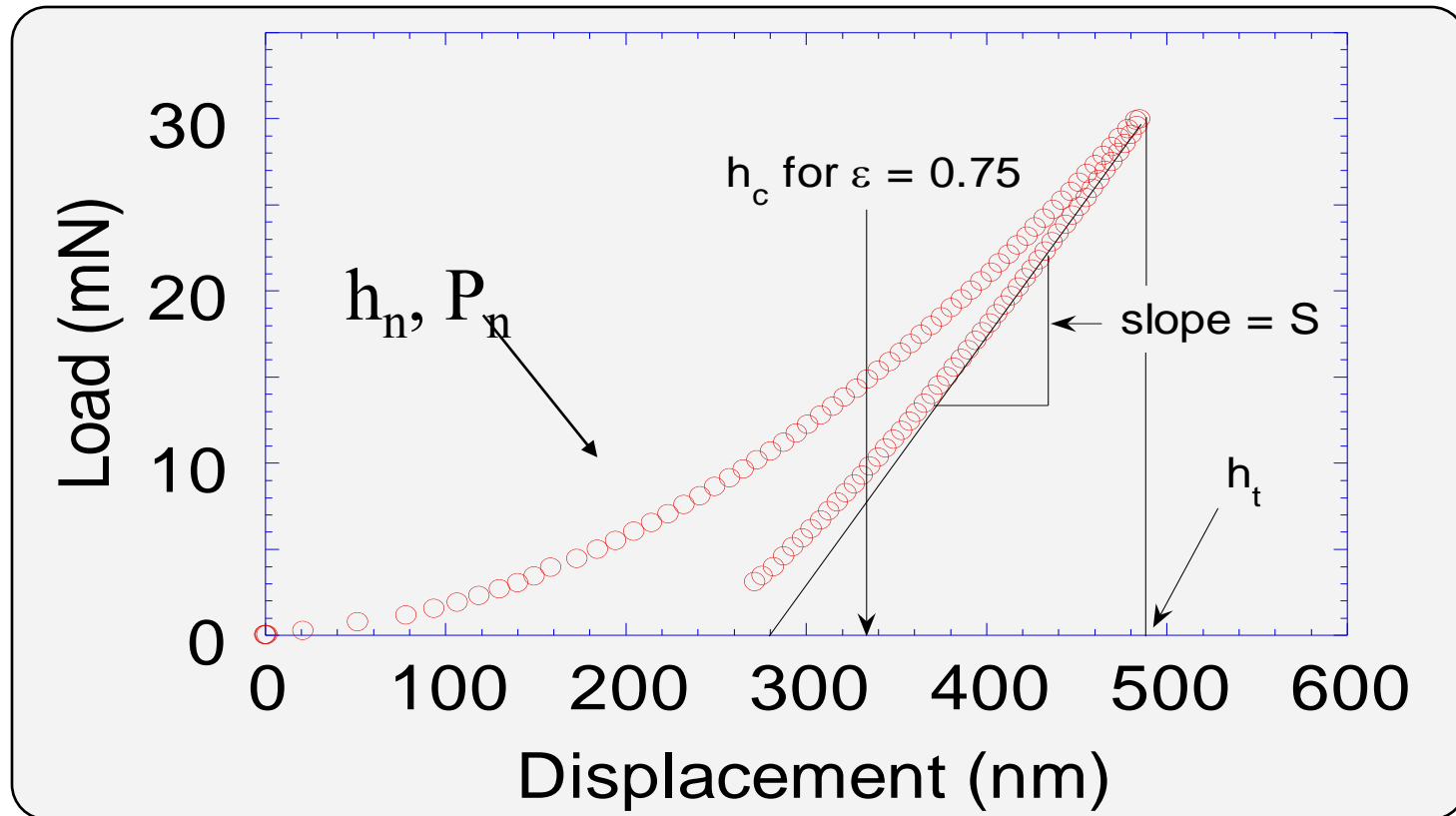
Warren C. Oliver
President



NANO Indenter[®] G200 (XP or DCM) Schematic



Stiffness From Unloading



Summary of IIT (Nanoindentation) Analysis

$$\frac{1}{E_r} = \frac{(1-\nu^2)}{E} + \frac{(1-\nu_i^2)}{E_i}$$

$$\sigma_y \approx H/3$$

$$H = P/A$$

$$E_r = \frac{\sqrt{\pi}}{2} \frac{S}{\sqrt{A}}$$

$$A = f(h_c)$$

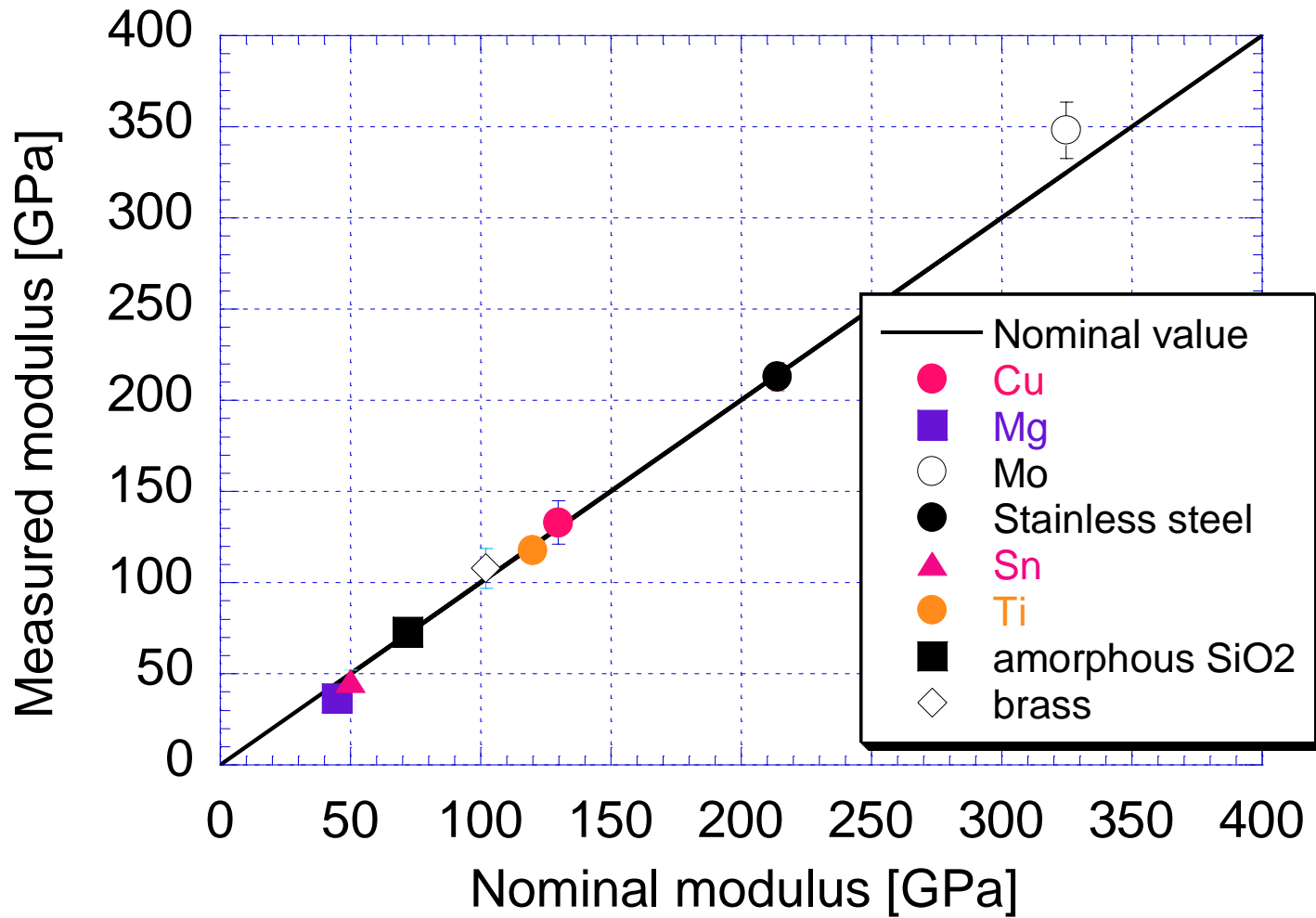
$$h_c = h - 0.75P/S$$

$$S = \left. \frac{dP}{dh} \right|_{h_{\max}}$$

Nomenclature:

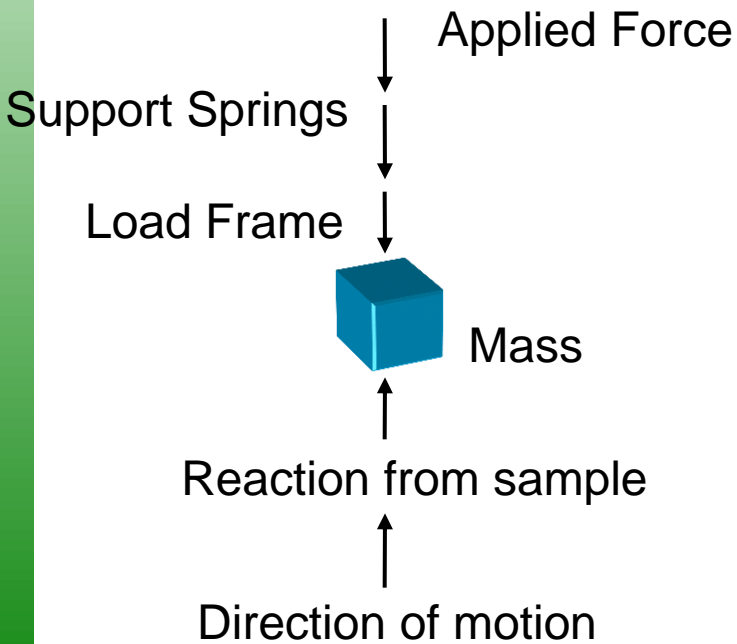
E	Young's modulus
H	hardness
σ_y	Yield stress
E_r	reduced modulus
ν	Poisson's ratio
i	(as subscript) indenter
S	contact stiffness
A	projected contact area
h_c	contact depth
h	displacement
P	applied force (load)

Getting Young's Modulus by Indentation



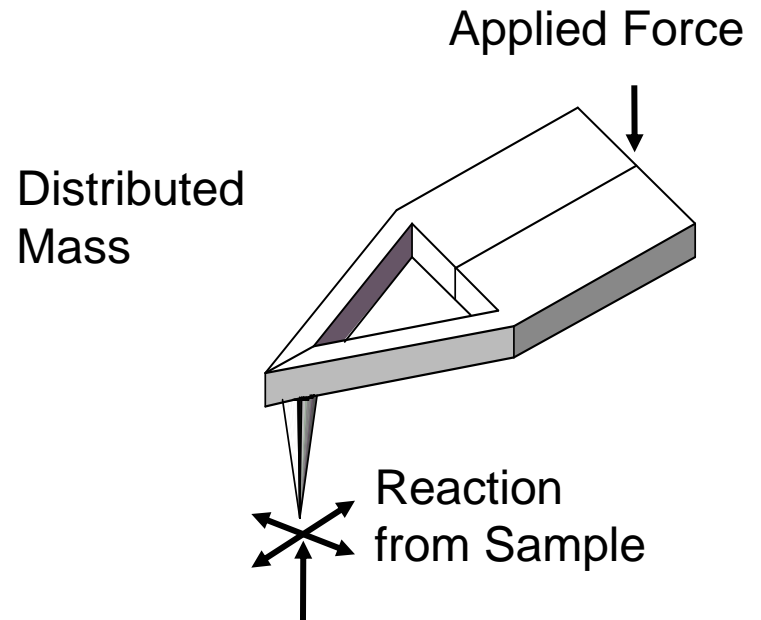
One Dimension vs Many

Two Springs - One Dimensional Motion



Quantitative

One Spring or a Cantilever - Many dimensions

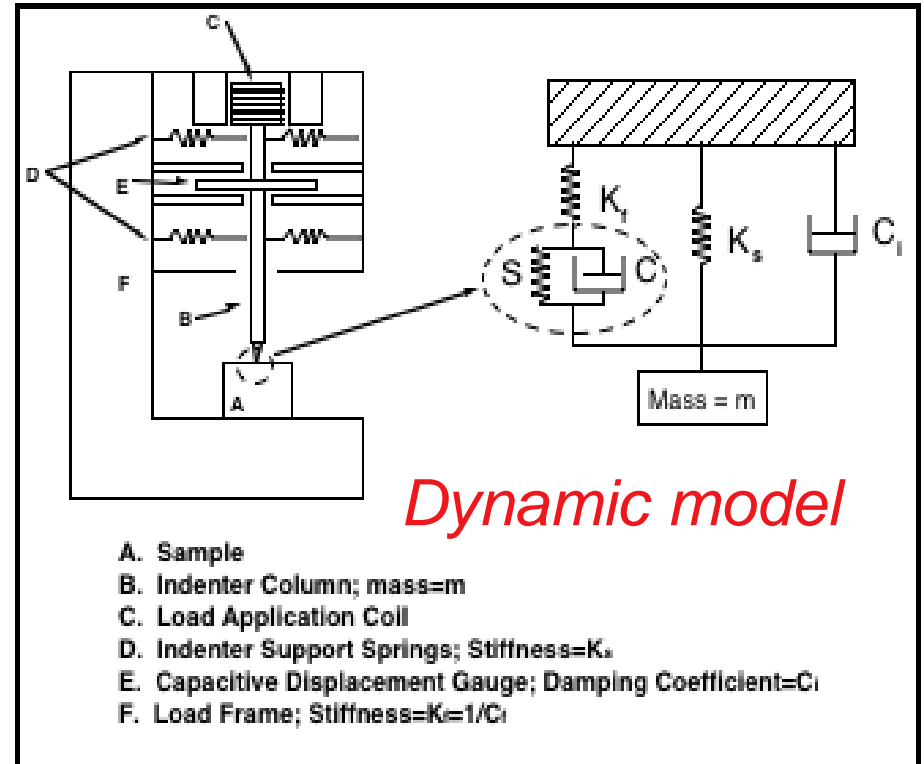
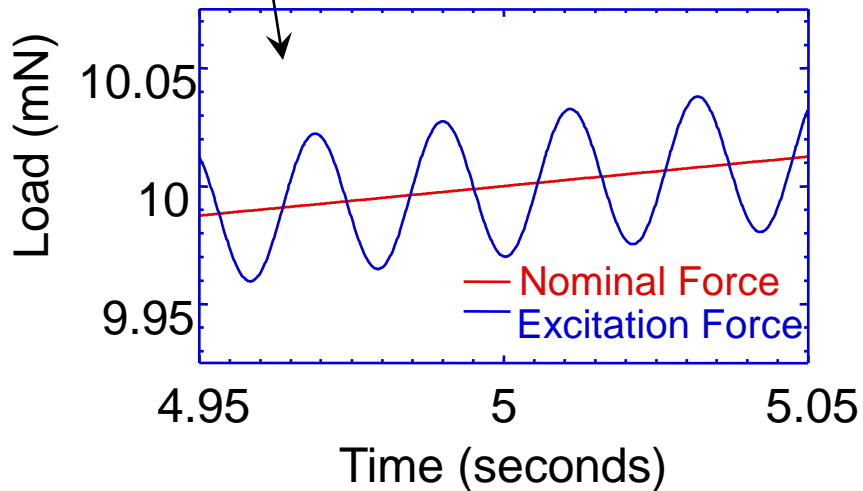
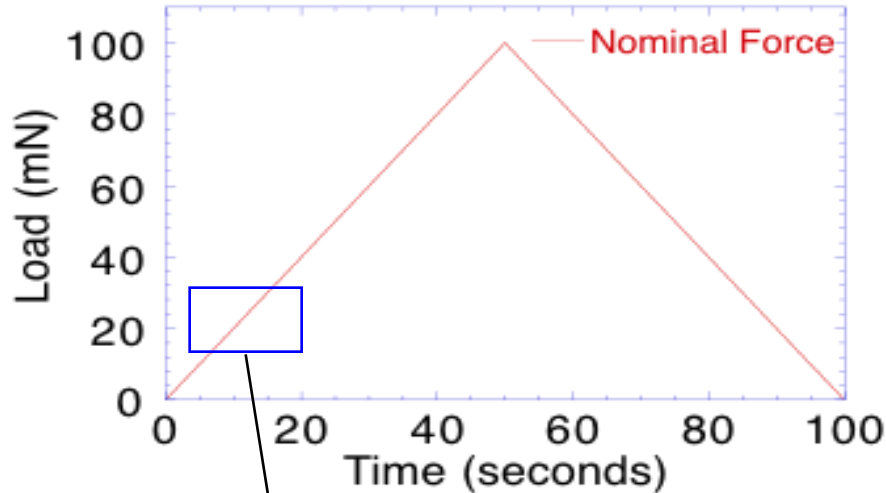


Many modes of vibration and multiple degrees of freedom

Difficult to Analyze

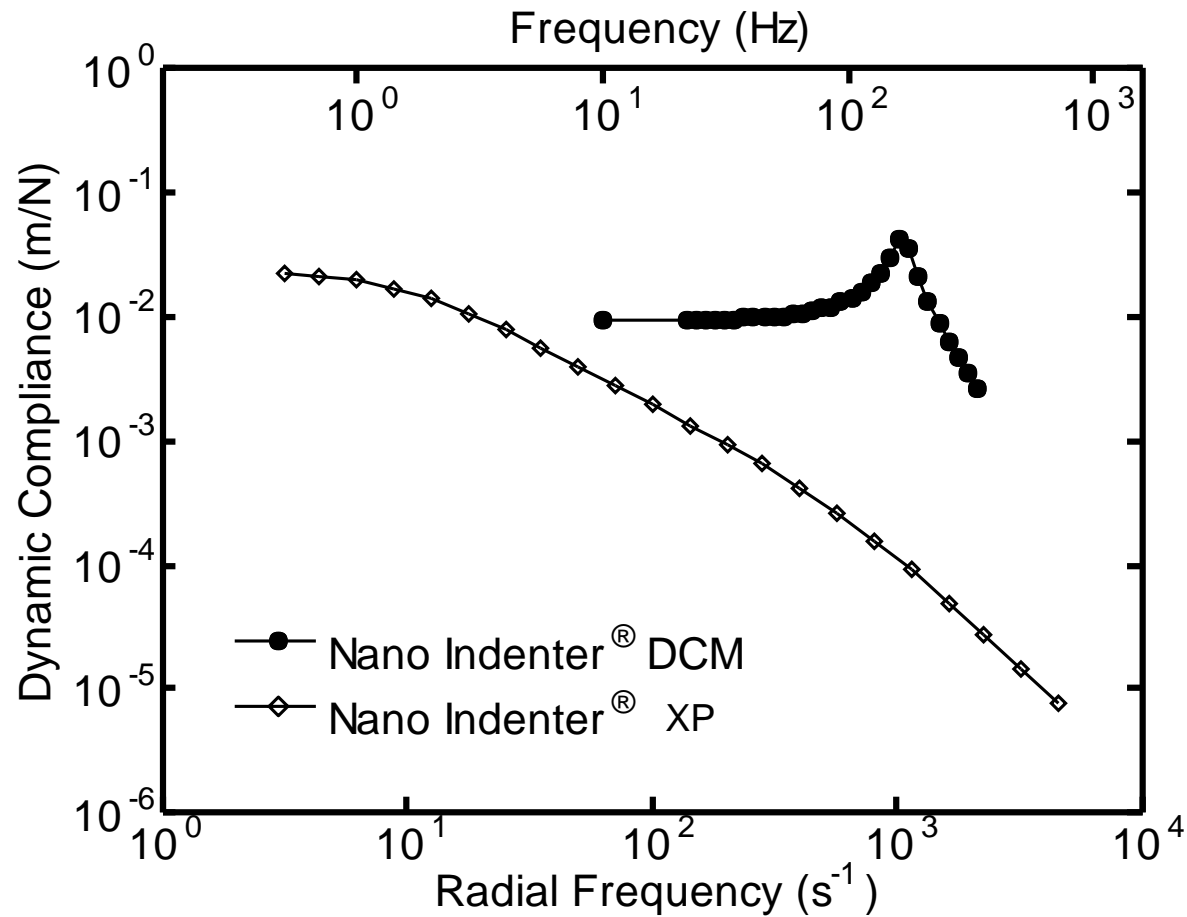
Continuous Stiffness Measurement

• Oliver & Pharr, *J Mater Res*7, 1564 (1992)

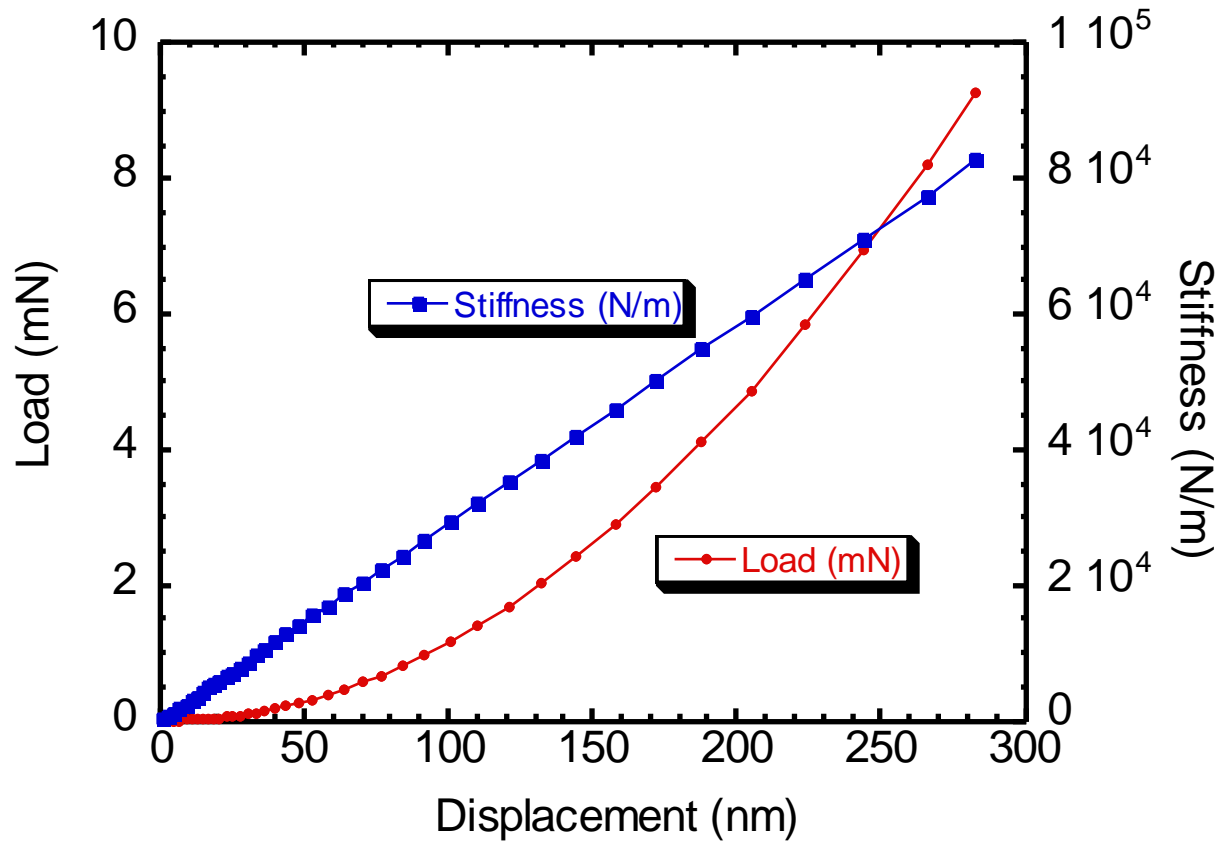


Measurement Actuator Dynamics

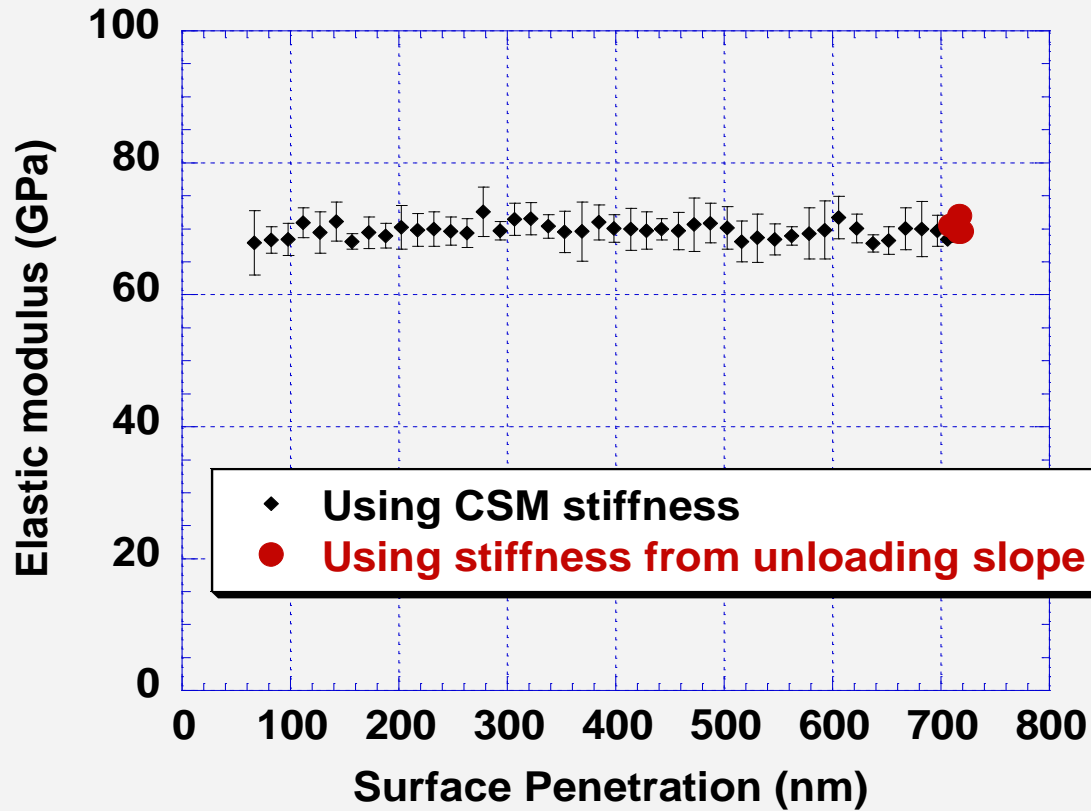
	<i>XP</i>	<i>DCM</i>
K_s (N/m)	80	100
m (gm)	10	0.01
C_i (N/m/s)	4	0.01



Stiffness from CSM

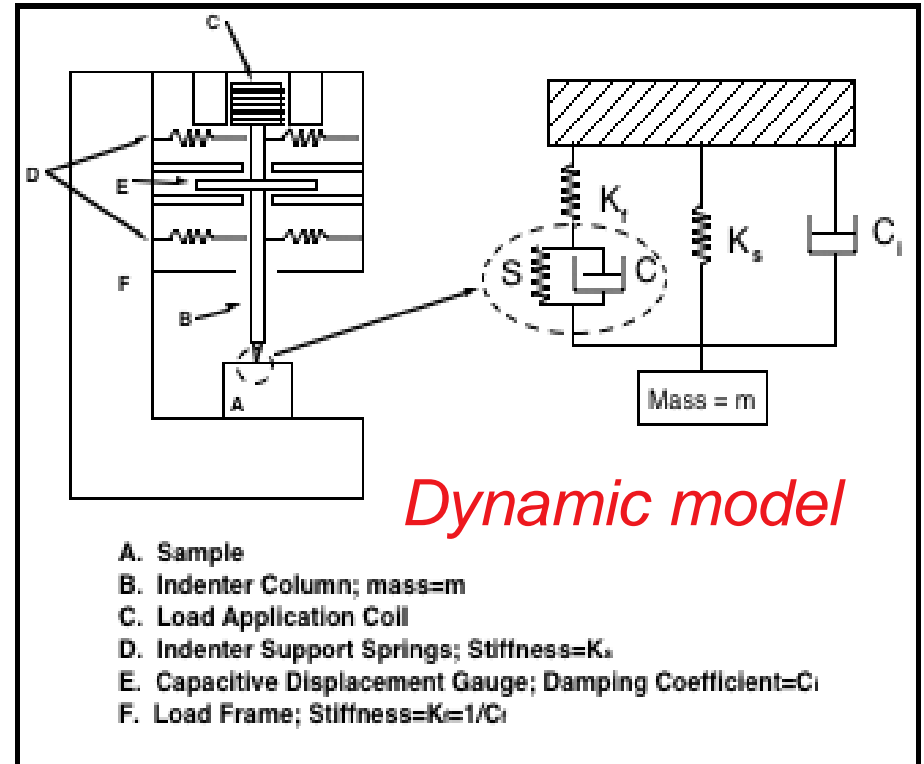
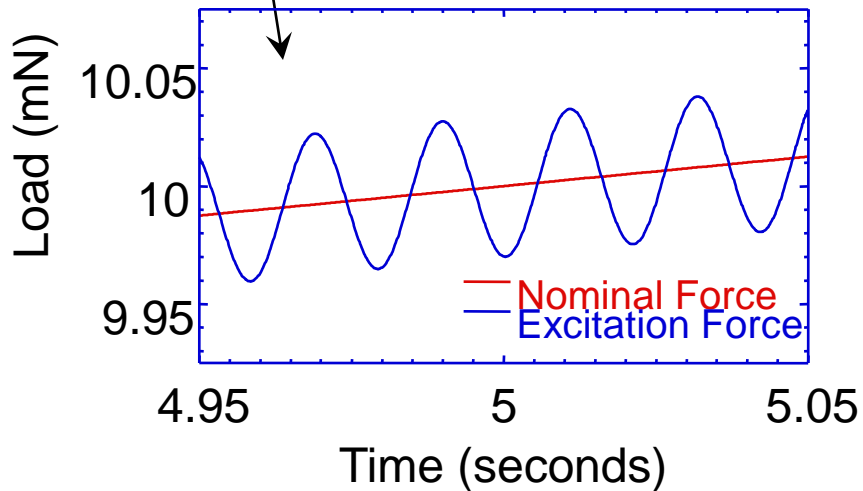
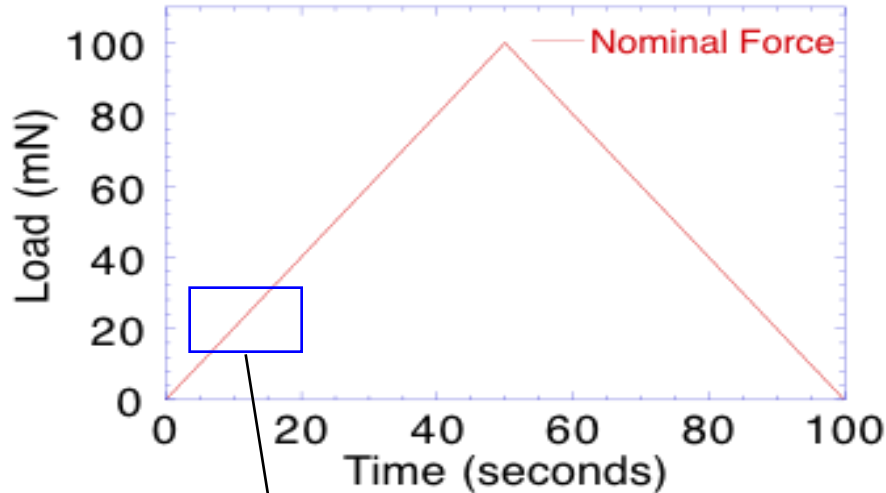


Elastic Modulus on Fused Silica



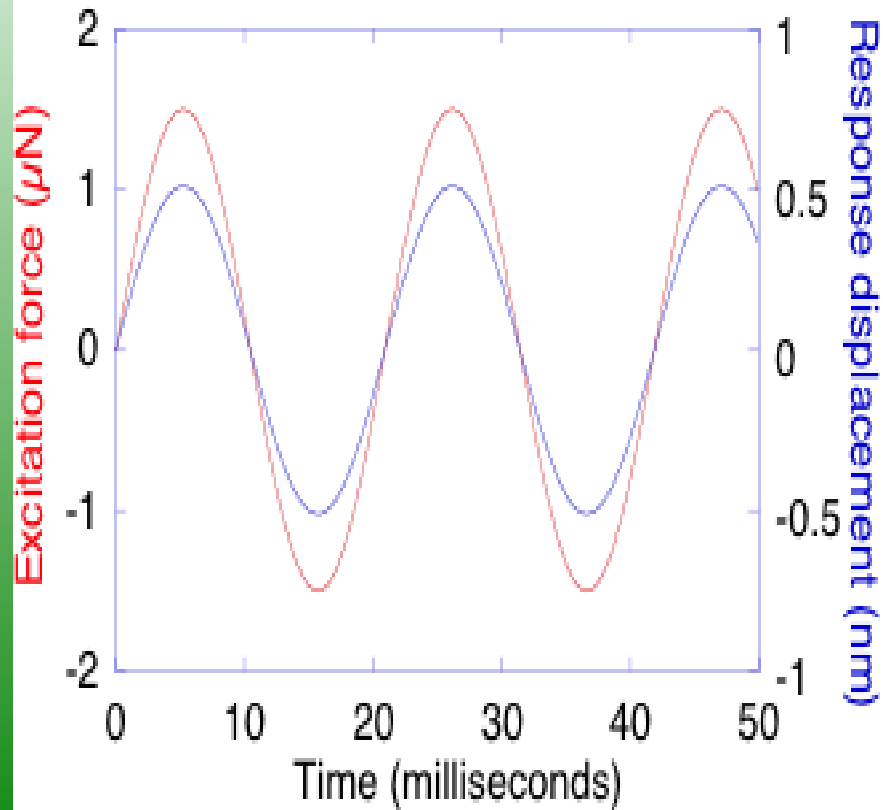
Continuous Stiffness Measurement

• Oliver & Pharr, *J Mater Res*7, 1564 (1992)

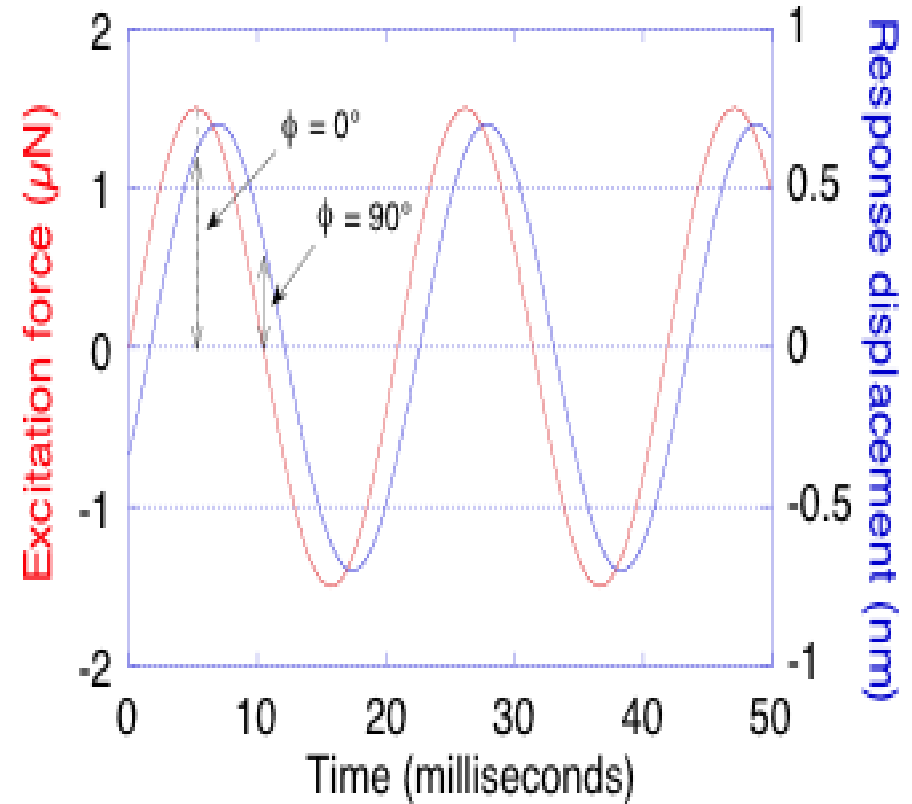


Material Response

Elastic

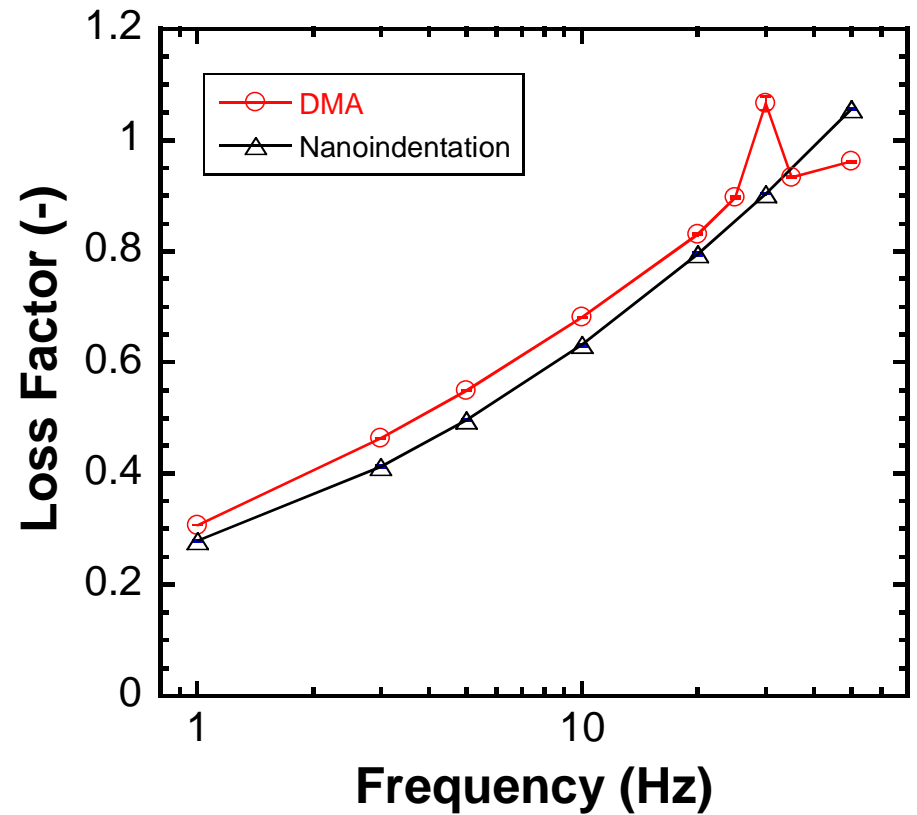
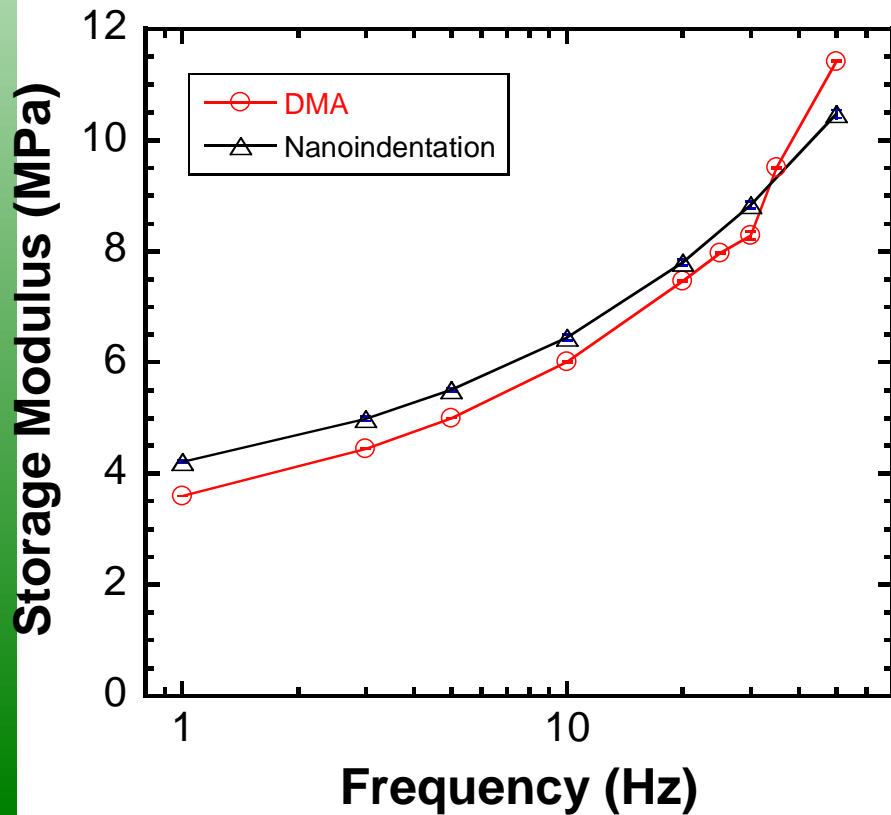


Viscoelastic

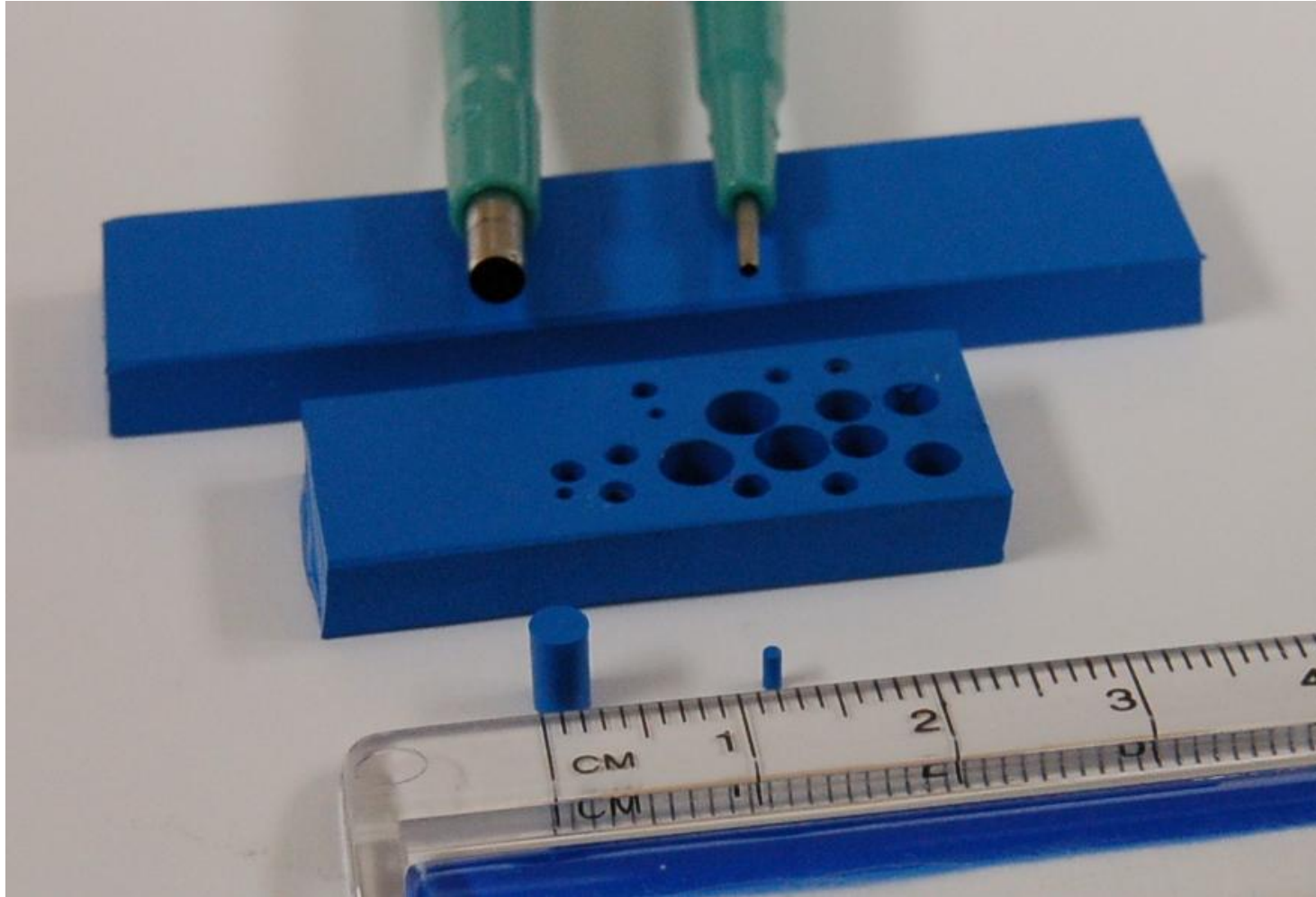


DMA VS. Nanoindentation

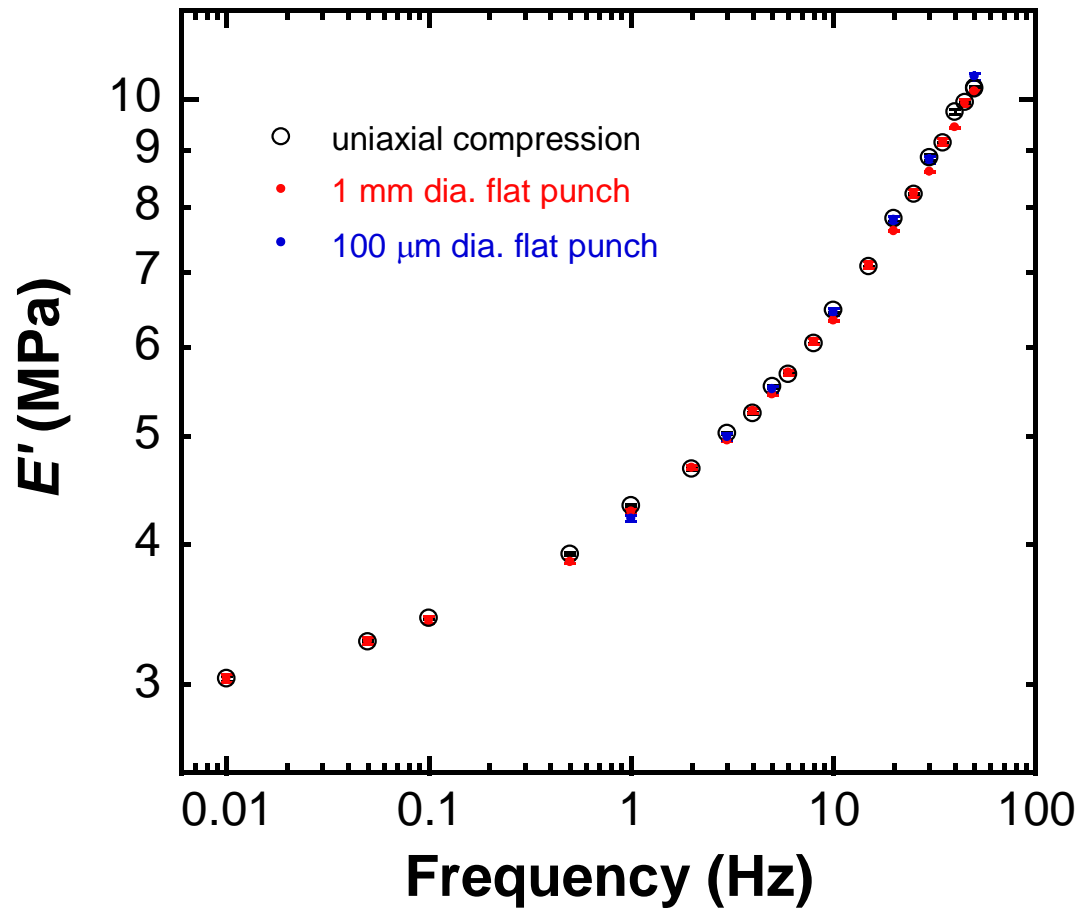
Highly plasticized polyvinylchloride,
the complex modulus at 22 °C



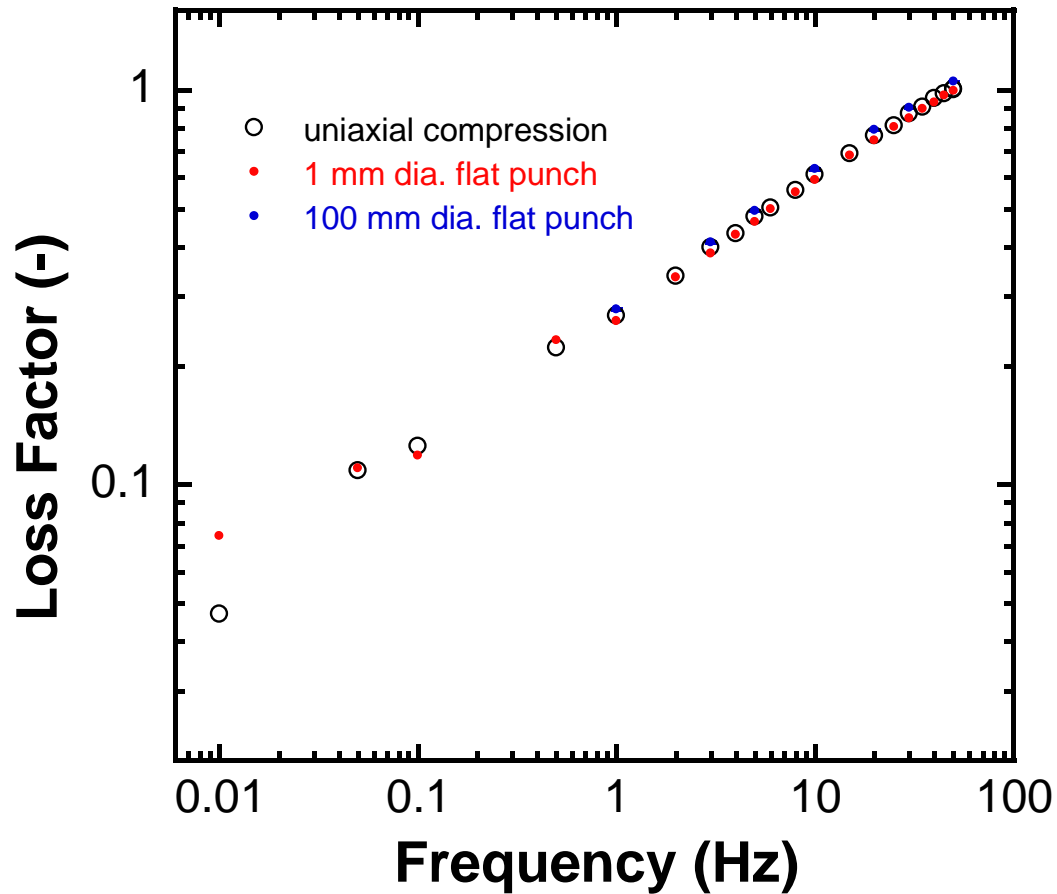
Compression Samples



Compression & Indentation



Compression & Indentation



QUESTIONS?

